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Persistence in inequalities across the Spanish regions

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Abstract: This paper investigates several issues concerning persistence in inequalities of relative income per capita among the Spanish regions over 1980-2002. For that purpose we take a Bayesian approach which extends the work by Canova and Marcet (1995). Firstly, we study to what extent there exists a fixed effect bias in the standard cross-section estimates, and we find that the speed of convergence is indeed underestimated. Secondly, we provide a battery of results in which steady states and convergence rates have been obtained for a continuum of prior distributions. Finally, we also deal with persistence in inequalities by determining whether initial conditions matter in the distribution of regional steady states, and our conclusion is that regional disparities tend to persist over time in Spain.

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1 Introduction

Debate among economists and policy makers on the existence of convergence across countries and regions remains on the table. On the basis of the textbook Solow model, a huge number of empirical studies have been carried out to elucidate not only whether economic convergence exists but also which factors should be identified as engines of growth. A relevant part of this literature is motivated by the following questions: Will disparities in income per capita disappear as time goes by? What is the speed at which this convergence process takes place? Can governments follow adequate policies to increase growth rates or, by contrast, are economies doomed to keep their positions in comparative rankings?

The standard approach in growth empirics is running cross-section regressions à la Barro. Barro and Sala-i-Martin (1992) and Mankiw *et al.* (1992) detect convergence in several samples and estimate a speed of convergence of about 2% a year. However, an important caveat has to be kept in mind when assessing such results and those coming from subsequent literature: the analysis is based on the assumption that steady states and speeds of convergence are the same for all economies involved in the sample. Indeed, a seminal paper by Islam (1995) showed the existence of a fixed effect bias arising from regressions that do not control for heterogeneity across units. The main consequence of allowing for such a degree of heterogeneity is a substantial increase in the convergence rates, which achieve values of about 9%. This finding has been confirmed by other papers such as Canova and Marcet (1995), Caselli *et al.* (1996) and Maddala and Wu (2000).

On the other hand, De la Fuente (1998) has warned against an excessive confidence in estimates stemming from panel data methods. His argument is based on the difficulty of distinguishing between short-term fluctuations and long-term growth dynamics when panel data are involved. He points out that the use of (relatively) high frequency data is proved to generate misleadingly high estimates of the speed of convergence as a result of a short-term noise in the series.

In this article we follow the works by Canova and Marcet (1995), Maddala and Wu (2000) and Canova (2004), who applied Bayesian techniques to the analysis of the persistence in inequalities among European regions and OECD countries. Particularly, we borrow from Canova and Marcet (1995) the idea of exchangeability on some key parameters of the model. In turn, we slightly extend their Bayesian technique in three directions. Firstly, the speeds of convergence will be truncated on the unit circle, that is, the equations will be forced to revert to a long run level. Secondly, we assume that the variance matrix of the residuals is non-diagonal, due to the presence of cross correlations among the equations of the system. Canova and Marcet (1995) instead assume this matrix to be diagonal and estimate it using maximum likelihood principles. Thirdly, once the Bayes rule is applied, we will use the Gibbs sampling method to obtain a numerical approximation of the marginal distributions of the parameters.

By extending the Bayesian techniques proposed by Canova and Marcet (1995), one of the main aims of the paper is to investigate the persistence in inequalities in the Spanish regions over the period 1980-2002. This covers the eighties and nineties which are the years in which a sudden stop in regional convergence has been detected in Spain (see, for instance, López-Bazo *et al.*, 1999).

This contrasts with the extended claim that convergence rates increase during the expansionary stages of the cycle. Along these lines, this paper provides additional evidence on this issue as our sample includes one of the lengthiest expansionary period in decades.

Two main questions are taken on board in our analysis. Firstly, we check whether a convergence analysis for the Spanish regions using standard cross-section regressions appears to be contaminated by the fixed effects bias and, in a complementary manner, whether panel data estimates report excessively high speeds of convergence. In this regard, we study how the speed of convergence varies once we gradually alter the precision of the prior distribution of the parameters. At this point, we extend the contribution by Shioji (2004) by using his forecasting exercise in order to select the best prior assumptions on the distribution of relevant parameters. Secondly, we investigate the issue of persistence in inequalities across the Spanish regions and its sensitivity to the a priori econometric specification used. As a by-product, this will provide some insight on whether convergence is conditional or absolute.

Our main findings are as follows. Firstly, we corroborate previous findings by Canova and Marcet (1995) in the sense that the cross-section approach renders a biased estimate of the speed of convergence. In that regard, when steady states and speed of convergence parameters are not constrained to be common across regions, we find a much higher speed of convergence. Secondly, we strongly reject the hypothesis of unconditional convergence since regions are found to be converging to their own steady states rather than to a common steady state. Thirdly, we consistently find evidence of persistence in inequalities across the Spanish regions, showing that income differences have hardly narrowed down over the period under analysis. Thus initial conditions appear to be important in determining the relative position in the distribution of estimated steady states. These latter findings should be interpreted with caution since as stressed by De la Fuente (1998), panel data methods may show high sensitivity in the estimation of steady states depending on the length of the sample.

The rest of the paper is organized as follows. Section 2 describes the econometric methodology employed in the study. Section 3 presents a brief description of the data and the results of the analysis. A direct comparison of our approach with that of Canova and Marcet (1995) is also presented. Section 4 deals with the issue of persistence in inequalities and Section 5 presents the Montecarlo experiment used to choose among different prior distributions. Finally, Section 6 puts forward some policy implications and concludes.

2 Econometric method

This section presents the Bayesian tools used in this paper. The model to estimate is an N -equation Gaussian panel with an $AR(1)$ structure. Let y_{nt} denote (the log of) *per capita* income of region n (for $n = 1, \dots, N$) at time t relative to (the log of) the mean across regions in t , *i.e.*

$$y_{nt} = \log(Y_{nt}) - \log\left(\frac{1}{N} \sum_{n=1}^N Y_{nt}\right),$$

where Y_{nt} represents *per capita* income of region n at time t . The observation y_{nt} is then generated by

$$y_{nt} = \alpha_n + \rho_n y_{nt-1} + u_{nt}, \quad (1)$$

for $t = 1, \dots, T$. For equation n , stationarity requires $\rho_n \in (-1, 1)$, then mean reversion gives an equilibrium or steady state value for equation n equal to

$$SS_n = \frac{\alpha_n}{1 - \rho_n}. \quad (2)$$

In a growth context, $v_n = 1 - |\rho_n|$ is interpreted as the speed of convergence of region n to the *relative* steady-state. As ρ_n gets closer to the limits of the unit circle, the degree of mean reversion decreases. If ρ_n is equal to 0, any deviation from the equilibrium value is automatically corrected, given that the data generating process (1) is white noise. Accordingly, the term SS_n is interpreted as the difference of the n -th region's steady state from the national steady state. Hence, a negative value for SS_n means that the n -th region's steady state is below average, thereby implying that region n grows at a lower rate along the balanced growth path than the average does.

At any time t , residuals across equations are assumed to be serially uncorrelated and are distributed according to $u_t = (u_{1t}, \dots, u_{Nt})' \sim i.i.d. \mathcal{N}_N[0, \Sigma]$, for all t , where $\Sigma : N \times N$, is non-diagonal.

- **Assumption 1:** The data $y_n = (y_{n1}, \dots, y_{nT})'$ are generated by equation (1), for $n = 1, \dots, N$.
- **Assumption 2:** The value of ρ_n lies inside the unit circle, i.e., $\rho_n \in (-1, 1)$, for $n = 1, \dots, N$. Formally, $\rho_n \in S(\rho)$, for all $n = 1, \dots, N$, where

$$S(\rho) = \{\rho_n : |1 - \rho_n z| \neq 0, \forall z \in [-1, 1]\}. \quad (3)$$

Given these conditions and assumptions, the system of equations (1) can be reduced to the following expression

$$y = X\beta + u, \quad (4)$$

with $u \sim \mathcal{N}_{NT}(\mathbf{0}_{NT}, \Sigma \otimes I_T)$, and matrices in (4) have the form: $y = (y_1, \dots, y_N)'$: $NT \times 1$,

$$X = [(I_N \otimes \mathbf{1}_T), \text{diag}(y_{1,-1}, \dots, y_{N,-1})] : NT \times 2N, \quad (5)$$

with $y_{n,-1}$ denoting the one-period lagged matrix for region n , $T \times 1$. Matrix $\text{diag}(y_{1,-1}, \dots, y_{N,-1})$ is block diagonal, $NT \times N$, and $\beta = (\alpha_1, \dots, \alpha_N, \rho_1, \dots, \rho_N)'$: $2N \times 1$. This implies that the likelihood function is $y|\beta, \Sigma = p(y|\beta, \Sigma) = \mathcal{N}_{NT}[X\beta, \Sigma \otimes I_T]$.

2.1 Priors

Two blocks of parameters are to be estimated, β and Σ . We borrow from Canova and Marcet (1995) the idea of exchangeability for β , with a slight variation, namely, all the slopes ρ_n will be truncated into the stationarity set $S(\rho)$ defined in (3). In addition, we differ from Canova and Marcet (1995) in the prior set for Σ . In their work, a diagonal matrix for $\Sigma = s^2 I$ is proposed, where the scalar s^2

is derived from maximum likelihood estimation. In turn, the prior probability for the estimated s^2 is assumed to be 1. From a Bayesian perspective, this implies that Canova and Marcet (1995) pose an absolute confidence that the ML estimate of s^2 is the true value. This allows to directly extract the relevant posterior distribution for β .

In our case, we will not assume a diagonal prior on Σ nor employ maximum likelihood techniques for the choice of its value. Instead, we propose a Wishart distribution as prior for Σ , and then exploit the Bayes rule to compute the posterior for β and Σ . These posterior distributions, however, have the uncomfortable form that β is conditional on Σ and, at the same time, that the distribution of Σ appears conditional on β . In an attempt to overcome this problem, we will use a Montecarlo integration technique, *i.e.* the Gibbs sampling method, to produce a numerical approximation of the marginal (not conditional) distributions of β and Σ . We shall now explain the priors.

[β]: *Parameters.* Priors are said to be exchangeable if equations are sharing a common value of parameters, regardless the ordinality of equations. In our model (1), if equation n is assumed to have the same intercept and slope than some other *given* equation m , no matter if $n \leq m$, then under normality one may write

$$\alpha_n | \alpha_m \sim \mathcal{N}[\alpha_m, \sigma_\alpha^2], \quad \forall n \neq m, \quad (6)$$

$$\rho_n | \rho_m \sim \mathcal{N}[\rho_m, \sigma_\rho^2], \quad \forall n \neq m. \quad (7)$$

Expression (6) says that when equation m is given, equation n is expected to have the same intercept as m , with a precision represented by $1/\sigma_\alpha^2$, *i.e.* the inverted prior variance. As long as σ_α^2 approaches 0, an econometrician reveals to feel extremely confident about such a belief, the precision tends to zero, and intercepts are fully exchangeable between equations n and m in the system. The opposite happens when σ_α^2 tends to infinity. The prior for the slope parameter in (7) has an identical interpretation.

Canova and Marcet (1995) show that this is equivalent to imposing a prior on the difference of these parameters (see their appendix 3), that is

$$\alpha_n - \alpha_m \sim \mathcal{N}[0, \sigma_\alpha^2], \quad \forall n \neq m, \quad (8)$$

$$\rho_n - \rho_m \sim \mathcal{N}[0, \sigma_\rho^2], \quad \forall n \neq m. \quad (9)$$

where σ_α^2 and σ_ρ^2 are assumed to be given.

For the $2N$ β -parameters in the system, we shall assume a Gaussian prior, truncated to the set $S(\rho)$ in (3)

$$(I_2 \otimes R) \beta \sim \mathcal{N}_{(N-1)2}[\mathbf{0}_{(N-1)2}, (D \otimes \Omega)] \cdot S(\rho), \quad (10)$$

where $R : (N-1) \times N$, is a difference matrix given by

$$\begin{aligned} R(n, n) &= -R(n, n+1) = 1, \\ R(n, n-j) &= 0, \text{ for any } j \geq 1. \\ R(n, n+j) &= 0, \text{ for any } j \geq 2. \end{aligned}$$

The variance matrix is $D \otimes \Omega$,

$$D = \begin{bmatrix} \sigma_\alpha^2 & 0 \\ 0 & \sigma_\rho^2 \end{bmatrix} : (2 \times 2),$$

with $\Omega : (N-1) \times (N-1)$ and

$$\begin{aligned}\Omega(n, n) &= 1, \\ \Omega(n, n+1) &= \Omega(n+1, n) = -1/2, \\ \Omega(n, n+j) &= \Omega(n, n-j) = 0, \text{ for any } j \geq 2.\end{aligned}$$

Matrix Ω is so designed to prevent parameters from having variances that increase with the order of equations (see appendix 3 of Canova and Marcet (1995), where they show that matrix Ω makes the order totally neutral).

[Σ]: *Cross correlations*. A Wishart distribution will be assumed for the prior of Σ^{-1} ,

$$\Sigma^{-1} \sim \mathcal{W}_N[v_0, S_0]. \quad (11)$$

v_0 and S_0 are assumed to be known. If $v_0 = 0$ and $S_0^{-1} = \mathbf{0}_{N \times N}$, one imposes a non-informative prior for Σ^{-1} , where the posterior distributions will be led by the information content in the data set.

- **Assumption 3:** The prior distribution for the whole set of hyper parameters is given by

$$[\beta, \Sigma] = \mathcal{N}_{(N-1)2}[\mathbf{0}_{(N-1)2}, (D \otimes \Omega)] \cdot S(\rho) \times \mathcal{W}_N[v_0, S_0].$$

2.2 Posterior distributions and the Gibbs sampling

Under assumptions 1, 2 and 3,¹ the posterior for β , given Σ and the data set information, is $\beta|y, \Sigma \sim \mathcal{N}_{2N}[\beta_1, B_1^{-1}] \cdot S(\rho)$, where

$$B_1 = (D^{-1} \otimes R' \Omega^{-1} R) + X' (\Sigma^{-1} \otimes I_T) X, \quad (12)$$

$$\beta_1 = B_1^{-1} X' (\Sigma^{-1} \otimes I_T) y. \quad (13)$$

The posterior for Σ , given β and the data set information, is $\Sigma^{-1}|y, \beta \sim \mathcal{W}_N[v_0 + T, S_1]$, where $S_1 = [S_0^{-1} + S_u]^{-1}$, with $S_u = [s_{n,m}^u] : N \times N$ for $n, m = 1, \dots, N$, and

$$s_{n,m}^u = (y_n - \alpha_n - \rho_n y_{n,-1})' (y_m - \alpha_m - \rho_m y_{m,-1})$$

Notice that $\beta|y, \Sigma$ and $\Sigma^{-1}|y, \beta$ are *conditional* posterior distributions, that is, they both require some given conditional value from the other block. However, as we are rather concerned with the joint posterior distributions of β and Σ , these unconditional distributions can be obtained through the Gibbs sampling method. Here we provide a very basic description of this numerical algorithm.² Consider a sequence of steps labeled as $i = 1, \dots, I$. Then, for a given collection of initial conditions for $\{\beta, \Sigma\}$, which we denote $\psi_{(0)}$, set $j = 1$ and start the process as follows:

1. Draw $\beta^{(j)}$ from $\beta|y, \Sigma^{(j-1)}$.
2. Draw $\Sigma^{-1(j)}$ from $\Sigma^{-1}|y, \beta^{(j)}$.

¹Proof is available from the authors upon request.

²For a detailed description of this algorithm, see Casella and George (1992).

3. Call $\psi_{(j)} = \{\beta^{(j)}, \Sigma^{(j)}\}$, replace the step-index by $j+1 \leq J$, and go again to step 1 in the process. Otherwise, for $j = J+1$, stop the sampling.

This process should be iterated for J large, say $J = 15,000$, and after removing a “reasonable” number of initial draws on $\psi_{(j)}$, say $J_0 = 1,000$, the rest of draws can be used for inference and calculation of relevant moments, which are computed as follows:

$$\hat{\beta}_1 = \frac{1}{J - J_0} \sum_{j=J_0+1}^J \beta^{(j)}, \quad (14)$$

$$\hat{B}_1^{-1} = \frac{1}{J - J_0} \sum_{j=J_0+1}^J \left(\beta^{(j)} - \hat{\beta}_1 \right) \left(\beta^{(j)} - \hat{\beta}_1 \right)', \quad (15)$$

$$\hat{\Sigma} = \frac{1}{J - J_0} \sum_{j=J_0+1}^J \Sigma^{(j)}. \quad (16)$$

By using the weak version of the law of large numbers, for $J \rightarrow \infty$, these moments converge to the moments of the relevant marginal and joint distributions.

3 Results

3.1 Data

Our data set consists of per capita output series for the 17 Spanish regions over the period 1980-2002. More specifically, we use PPP per inhabitant gross domestic product at NUTS level 2 which is retrieved from the Regio data set of Eurostat. As it is well-known, the use of data defined at NUTS-2 level is preferable to a more aggregated definition as implied by NUTS-1 level data, which usually define broad regions comprising territories that are very different in terms of economic and socio-cultural structures. It is important to note that there has been a change in the base in 1995 and data are provided from 1980 to 1994 following ESA79, while data from 1995 onwards follows ESA95. Since that change may give rise to a break in the series, we have extended backwards the ESA95 series from 1994 to 1980 using the growth rates of per capita GDP calculated with the ESA79 series.

3.2 A helicopter tour

If a non-informative prior for Σ is assumed (i.e. $S_0^{-1} = \mathbf{0}$), the only priors that remain to be chosen is the pair $(\sigma_\alpha^2, \sigma_\rho^2)$. Assuming that $\sigma_\alpha^2 = \sigma_\rho^2 = 0$, we force the equations in the panel to share the same intercept and slope, that is, both parameters are fully exchangeable across equations. The system is then viewed as a single equation. If one sets $\sigma_\rho^2 = 0$ together with σ_α^2 increasing, there is only full exchangeability for the ρ'_n s across equations. As long as prior variances in $D = \text{diag}(\sigma_\alpha^2, \sigma_\rho^2)$ have values different from zero, both intercepts and slopes will start differing. Under the non-informative prior that $(\sigma_\alpha^2 \rightarrow \infty, \sigma_\rho^2 \rightarrow \infty)$, whatever resemblance among the α 's and the ρ 's across equations is a dictum from the data.

Figure 1 represents the positive orthant for the $(\sigma_\alpha^2, \sigma_\rho^2)$ hyper-parameter space. The choice of $(\sigma_\alpha^2, \sigma_\rho^2)$ is crucial for the estimation of the speed of convergence and steady state parameters. Under our Bayesian framework, three polar standard approaches can be written in terms of some specific priors: the cross-section (CS), the least square dummy variables (LSDV) and the seemingly unrelated (SUR) case. Empirical studies on growth and convergence usually adopt at least one of these three corner approaches. When both $(\sigma_\alpha^2, \sigma_\rho^2)$ approach 0, the system tends to be associated with the CS case, where all the equations in the system are forced to have the same intercept and the same speed of convergence. When the speed is set close to zero, thereby increasing the value σ_α^2 one gradually moves from CS to LSDV (i.e., $\sigma_\alpha^2 \rightarrow \infty$ and $\sigma_\rho^2 = 0$). Assuming a value of σ_α^2 tending to infinity, as long as the prior σ_ρ^2 is enlarged, one moves from LSDV to the SUR case where $(\sigma_\alpha^2 \rightarrow \infty, \sigma_\rho^2 \rightarrow \infty)$.

A grid of distributions will be presented where values for $(\sigma_\alpha^2, \sigma_\rho^2)$ are picked within an interval that goes from 10^{-6} up to 10^6 . The goal is to analyze how robust the estimate set β is along this tour.

Figure 1 about here

3.3 Speed of convergence to the steady states

In tables 1-3 we present the estimates of the speed of convergence for different models characterized by a broad range of values of σ_α^2 and σ_ρ^2 . In the three panels of table 1, we show the estimates for the three corner cases: CS, LSDV and SUR. The first of them restricts both the α_n and ρ_n parameters to be the same across regions as in the cross-section approach. Not surprisingly, the estimate of a common speed of convergence towards a common steady state appears very low (lower than 1%, nearly a unit root).

We then allow the intercepts to vary across regions (case where $\sigma_\alpha^2 = 10^6$ and $\sigma_\rho^2 = 10^{-6}$) as in those studies employing a fixed effects or LSDV estimator (see Islam (1995) and Caselli *et al.* (1996)). This renders a much higher speed of convergence to region-specific steady states as held by the conditional convergence hypothesis. The speed of convergence appears of the order of 40% a year, which seems to be an extraordinarily high value as compared to previous studies employing the LSDV estimator that rendered a speed not higher than 20%. In this regard, three issues are noteworthy. Firstly, as noted by Canova and Marcet (1995), when we do not appropriately account for the heterogeneity of intercepts across regions, the estimates of ρ are overstated (fixed effects bias), since the estimate of the parameter is pooled towards the cross-sectional mean, thus yielding low speeds of convergence. Secondly, we have found that the estimate of ρ is very sensitive to the number of iterations employed in estimating the variance-covariance matrix.³ In fact, when the FGLS estimator with only two iterations is used the value of ρ substantially increases, and consequently a convergence rate close to 20% is found. And thirdly, these extraordinarily high speeds of convergence may be related to the issue pointed out by De la Fuente (1998) concerning the influence of short-term noise on long-term growth dynamics.

Once we lift any restriction on the α_n and ρ_n parameters (SUR case where $\sigma_\alpha^2 = \sigma_\rho^2 = 10^6$), we obtain an average speed of convergence of around 35% which

³Results are available from the authors upon request.

is a bit higher than the 29% estimated by Lee *et al.* (1997) and substantially higher than the 23% estimated by Canova and Marcet (1995) for the European regions. Our estimates range from a low convergence speed of around 12% for Castile-La Mancha and Madrid to an extremely high value of almost 90% for Andalusia. This thus indicates that Andalusia adjusts almost instantaneously to any deviation of current income levels from steady state values. If we cluster the regions on the basis of their speed of convergence towards their steady states, we find that Castile-La Mancha, Castile-Leon, Madrid and Murcia appear to converge at a speed lower than 20% per annum. Regions with a convergence speed in the range of 20 – 40% are Asturias, Baleares, Cantabria, Catalonia, Canary Islands, Extremadura, La Rioja and Valencia. The Basque Country, Aragon and Galicia appear to converge at a rate between 40 and 60%, and Navarra and Andalusia converge at a rate above 60%.

In table 2, we further explore how the speed of convergence behaves in a range of intermediate cases between the cross-section and the LSDV cases. We do that by setting $\sigma_\rho^2 = 10^{-6}$ and gradually increasing σ_α^2 from 10^{-5} to 1. We observe that the speed of convergence gradually increases from a low 0.5% when $\sigma_\alpha^2 = 10^{-5}$ to 40% when $\sigma_\alpha^2 = 1$, which is pretty much similar to the case when $\sigma_\alpha^2 = 10^6$. In table 3 we explore the intermediate cases between the LSDV and the SUR approach by setting $\sigma_\alpha^2 = 10^6$, and gradually increasing the value of σ_ρ^2 from 10^{-5} to 1. We find that the average speed of convergence takes on a value of 40% when $\sigma_\rho^2 = 10^{-5}$ and decreases to about 32% when $\sigma_\rho^2 = 10^{-3} = 10^{-2}$, and again increasing to about 41% when $\sigma_\rho^2 = 1$.

Taken as a whole, we find evidence of the fixed effect bias associated with the cross-section approach, which tends to pull the estimated speed of convergence to a very low value. Once we allow the intercepts and slope coefficients to vary, we find overwhelming evidence that the average speed of adjustment is much higher than that previously found in the literature based on cross-section regressions. An average speed of convergence of around 35% a year implies that regions quickly adjust to any shock leading current income levels to deviate from their expected steady state values. It could also be the case that short-term cyclical fluctuations lead to excessively high speed of convergence estimates.

Tables 1, 2 and 3 about here

3.4 A comparison of strategies

In this subsection we present an evaluation on the gains from using our bayesian methodology with respect to that introduced by Canova and Marcet (1995). In their work, the posterior mean has the standard form

$$\beta_{CM} = [(D^{-1} \otimes R' \Omega^{-1} R) + X' (\Sigma^{-1} \otimes I_T) X]^{-1} X' (\Sigma^{-1} \otimes I_T) y, \quad (17)$$

where the matrix Σ is assumed to be diagonal, $\Sigma = s^2 I$. The remaining matrices D , R and Ω , are defined as before. Notice that this posterior mean is now a function of the scalar s^2 , $\beta_{CM} = \beta(s^2)$. The log-likelihood function can be expressed as

$$\begin{aligned} \log \ell(s^2) &= -\frac{NT}{2} \log(2\pi s^2) - \frac{1}{2s^2} u(s^2)' u(s^2), \\ \text{with } u(s^2) &\equiv y - X\beta_{CM} = y - X\beta(s^2). \end{aligned} \quad (18)$$

Suppose that s^2 is selected so as to maximize function $\log \ell(s^2)$ in (18), and in turn the prior probability for the estimated s_{ML}^2 is assumed to be 1,

$$\begin{aligned} s_{ML}^2 &\equiv \arg \max \log \ell(s^2), \\ \text{prior}(s_{ML}^2) &= 1. \end{aligned}$$

Then, (17) takes the form of an *unconditional* exact posterior mean.

Table 4 reports calculations according to this strategy for the same stream of priors used in previous subsections. Thus, the central panel of the table reports the estimate of s^2 , as well as the log-likelihood and the speed of convergence as averaged across the regions. Provided that these speeds coincide with those reported by Canova and Marcet (1995), we shall be able to reproduce their results. Yet, the rightmost panel reports the log-likelihood according to our Gibbs-bayesian strategy as well as the speed of convergence, collected in previous tables. This log-likelihood has been computed using the posterior unconditional means computed by the Gibbs sampler (see expressions (14) to (16)). As this log-likelihood is always higher than that of Canova and Marcet, we believe that this serves to justify that the strategy proposed in this paper presents an improvement of this method in terms of likelihood. Provided that twice this difference is distributed as χ^2 with $d.f. = N(N+1)/2 = 153$, the null hypothesis that matrix Σ is of the form $s^2 \times I$, is strongly rejected.⁴ Interestingly, note also that there are sensible differences in the estimates of the speeds of convergence, mainly when we move away from the region of CS-alike priors. Indeed, within the region of LSDV priors, our estimates of the speed of convergence double those estimated according to Canova and Marcet strategy (20% *versus* 40%!).

Table 4 about here

4 Persistence in inequalities

Table 5 and Figure 2 provide some descriptive evidence that will be helpful in supporting one of our arguments, *i.e.* the persistence in inequalities in the Spanish regions. Two different sources of Spanish relative *per capita* income are confronted: that of BBVA for 1955 and 1979 (a widely used biannual data source of Spanish income) *versus* that of Eurostat (actually used in this paper) for 1980 and 2002. Indeed, as was pointed out in the Introduction, we verify that an important stop in the convergence process took place in the late seventies. While the standard deviation of relative income per capita of 1955 achieved a value of 0.3690, this statistic takes a value of around 0.2209 in 1979, and it remains at this level over the next two decades (the average value is $\sigma_y = 0.2127$). This stability exhibited by the standard deviation leads to the statement that inequalities may have remained unaltered throughout 1980-2002.

In addition, in a more rigorous attempt to establish whether or not there is persistence in inequalities across the Spanish regions, we examine whether region-specific steady states are determined by initial conditions. For that purpose, we estimate simple OLS regressions of the type: $SS_n = a + by_{n,1980} + \xi_n$,

⁴Results not shown here. The likelihood in (18) assumes $N(N+1)/2 = 153$ restrictions on Σ (call it $\log \ell_R$). In our log-likelihood Σ is instead unrestricted (call it $\log \ell_U$). Hence $2(\log \ell_U - \log \ell_R) \sim \chi_{153}^2$.

where SS_n is the estimated steady state defined in (2) and $y_{n,1980}$ stands for the log of relative *per capita* output at the beginning of the period. We are particularly interested in the size of b , since the closer its value to 1, the more evidence there is for persistence in inequalities.⁵

Table 6 shows the results. The first specification uses as dependent variable the steady states estimated for the case of a common value for the α'_n s and ρ'_n s across regions. This renders a statistically insignificant estimate of b of around 0.38, which implies that regional differences in income levels will not persist forever and eventually disappear. However, the fit of the CS specification is quite poor with an R^2 below 10%. As we move from the cross-section approach towards the LSDV case, the size of b increases up to a statistically significant value of about 0.95 which implies almost perfect persistence in inequalities across the Spanish regions. The fit of the regressions is very good with R^2 's of almost 90%. If we further let the slope coefficient vary across regions, the average estimate of b slightly falls to 0.94 but remains significant at the 1% level and the R^2 remains about 85%. This again indicates the existence of almost perfect persistence in inequalities, with only a small reduction in income inequality occurring in the limit.

These findings should be interpreted with some caution, since as pointed out by De la Fuente (1998), the analysis of persistence in inequalities is problematic under a panel data framework. More specifically, De la Fuente (1998) finds that the estimated steady-states are either too erratic or tend to replicate the end-of-sample values of the income per capita series. Our results are consistent with this latter possibility, since the standard deviation of relative income per capita in 2002 is about 0.2059, while the same statistic computed for the estimated steady states under the assumption of a fixed effect model yields a value of 0.2100.

This fact leads to the reconsideration of the use of panel data estimates as a way to test the existence of conditional or unconditional convergence, since LSDV estimates do not seem to be very reliable to ground absolute convergence analyses due to the biased estimate of the steady-states. By contrast, other estimators such as the usual OLS may be more appropriate for dealing with this issue. So in line with De la Fuente (1998), we cannot totally rule out the possibility that our evidence of the persistence of regional disparities is not due to the use of panel data estimation methods.

Tables 5 and 6 and Figure 2 about here

5 Too many priors?

Following partially Shioji (2004), we have carried out a simple simulation exercise in order to select which prior distribution gets a better fit to the actual data generating process. The data point of BBVA regional per capita income for 1955 is considered to be a referential initial point. We use this reference point in order to check which of the available fifteen models defined for a different set of priors (as shown in tables 1, 2 and 3) displays the best accuracy for predicting

⁵A value of b equal to 1 would indicate that the position of the distribution of regional steady states has remained unchanged, and those regions beginning with a low steady state relative to national levels will not improve their relative position.

the first observed period in the Eurostat series, 1980. For each prior, we use the posterior marginal distributions (14), (15) and (16) to generate random draws of $\left\{ \alpha_n, \rho_n, \alpha_n / (1 - \rho_n), [u_{nt}]_{t=1956}^{1980} \right\}_{n=1}^{N=17}$. This step is repeated 15000 times, for any of which we calculate projections for 1980 $\hat{y}_{1980}^{(h,j)} = \left(\hat{y}_{n,1980}^{(h,j)} \right)_{n=1}^{N=17}$, where the superindex (h, \cdot) stands for the particular iteration (for $h = 1, \dots, 15000$) and (\cdot, j) labels the model ($j = 1, \dots, 15$). Then, we calculate the following distance to the observations in 1980, $y_{1980} = (y_{n,1980})_{n=1}^{N=17}$

$$d(j, y_{1980}) = \sqrt{\frac{1}{15000} \sum_{h=1}^{15000} \left[\frac{1}{17} \sum_{n=1}^{17} \left(\hat{y}_{n,1980}^{(h,j)} - y_{n,1980} \right)^2 \right]}.$$

This represents the root of the mean square errors. Model (j) is said to better fit y_{1980} than model (j') if $d(j, y_{1980}) < d(j', y_{1980})$, that is, if the projections from model (j) are closer to 1980 than the projections from (j') . In a similar manner we also calculate a measure of the distance of the projections to the steady states, $d(j, SS)$.

Table 7 shows that the prior distribution providing the best matching is that of $\sigma_\alpha^2 = 10^6$ and $\sigma_\rho^2 = 10^{-4}$, that is, a distribution based on a prior close to the underlying assumption in LSDV estimation. It corresponds to a mean value for ρ of 0,5394, that is, a speed of convergence of 46,06%. Again, due to the underlying heterogeneous value of α across regions, this high speed has to be interpreted as the adjustment of regional economies to *their own* steady states.

In terms of $d(j, y_{1980})$, it is also interesting to show how the matching capability decreases by a higher extent when the model specification is closer to the assumptions of cross-section analysis than when a more flexible probability distribution for the relevant parameters is considered. Note that the distance d is about three times higher under a cross-section approach than with LSDV estimates. In line with previous contributions and the results presented above, this is a clear argument in favor of taking into account a high degree of heterogeneity especially in terms of steady states.

When comparing columns for $d(j, y_{1980})$ and $d(j, SS)$, a lower value for the latter is found provided one goes from CS to SUR through LSDV. Shioji (2004) uses US state output data and also concludes that LSDV projections are closer to steady states than to actual observations. He thus interprets this result as a symptom that LSDV tend to overestimate the speed of convergence. In our view, this is a natural consequence of using the high speed convergence model as implied by the LSDV assumptions, *i.e.* the degree of mean reversion is so high that regions need no more than two years to correct deviations from their long run positions. So, in 25 years, from 1955 up to 1980, regions may have crossed over their steady state lines for about 10 to 12 times. However, a 2% speed would require 35 years for a half of the initial gap to vanish.⁶

Table 7 about here

⁶Anyway, the results show in the column heading by $d(j, SS)$ must be interpreted with caution, as long as the estimated steady states might be biased (De la Fuente, 1998).

6 Concluding remarks

In this article we have applied bayesian techniques to the analysis of the persistence in inequalities among the Spanish regions over the period 1980-2002. As mentioned above, our methodology tries to overcome the difficulties posed by the standard cross-section approach which neglects the within variation of the data and forces the speed of convergence to be the same across units. Our analysis thus allows for a high degree of heterogeneity across units, thus rendering estimates of region-specific steady state and speed of convergence parameters.

Our study has dealt with two main questions. Firstly, we have checked for the existence of a non-negligible fixed effects bias in cross-section regressions and whether panel data estimates report excessively high speeds of convergence. Second, we have investigated the issue of persistence in inequalities across the Spanish regions by determining to what extent steady state income levels are or not determined by initial conditions.

Our main findings have been the following. First, we have corroborated previous findings by Canova and Marcet (1995) in that the CS approach renders a biased estimate of a homogenous speed of convergence below 1% a year, which would be consistent with a Solow model with a very high capital share leading to a very slow adjustment along the transitional growth path. Second, when steady states and speed of convergence parameters are not constrained to be common across regions, we have found a much higher speed of convergence. Our estimates of the speed of convergence have appeared to range from a “low” value of around 12% a year for Castile-La Mancha and Madrid to almost 90% for Andalusia. This indicates that the latter has been permanently on its steady state.

Third, we have rejected the hypothesis of unconditional convergence since steady states have been found to significantly differ across regions. Fourth, our Gibbs-based bayesian approach has produced a larger likelihood than the approach suggested by Canova and Marcet (1995). Differences have also appeared in terms of the estimates for the slopes and intercepts.

Fifth, we have provided consistent evidence of persistence in inequalities across the Spanish regions, showing that income differences have hardly narrowed down over the period under analysis. Thus initial conditions have been the most important determinant of the relative position in the distribution of estimated steady states. At this point, a word of caution is necessary when interpreting our results, since as stressed by De la Fuente (1998) panel data methodology may render estimated steady states which are very sensitive to the features of the sample. Finally, replication of Shioji’s experiment has revealed that the best performance is achieved when one uses a prior distribution within the LSDV-alike prior, *i.e.* equal speeds of convergence although different intercepts across equations. Regions are found to converge at a speed of 40% – 46% to extremely different relative steady state levels.

The main results of the paper are consistent with previous contributions. In particular, high convergence rates have been also reported in Cuadrado (1998) -between 27% and 35% for the Spanish regions over 1980-1995- and De la Fuente (2002) -between 25% and 39% for 99 EU regions in the period 1980-1994. Along these lines, our results back up the finding of extremely high speeds of convergence towards region-specific steady states. These high convergence rates are compatible with a low share of private capital over output, with perfect private

capital mobility across regions, and with a very close position of economies to their steady states.

Taken as a whole, our results may point to the failure of EU regional policies instrumented through Cohesion and Structural Funds as a means for correcting regional disparities in Spain over the last decades. The absence of convergence has taken place despite the fact that growing resources have been allocated to the reduction of territorial income differences. Indeed, financial resources aimed at promoting convergence now account for over 30% of total EU budget, more than twice the share they represented in 1988. This lack of convergence casts doubts on the effectiveness of European development policies precisely when the EU enlargement leads to new challenges in the recipient territories. Therefore, our study also contributes by adding new arguments to the debate on the impact of regional policies.

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Figure 1: A helicopter tour over the Hyperparameter space

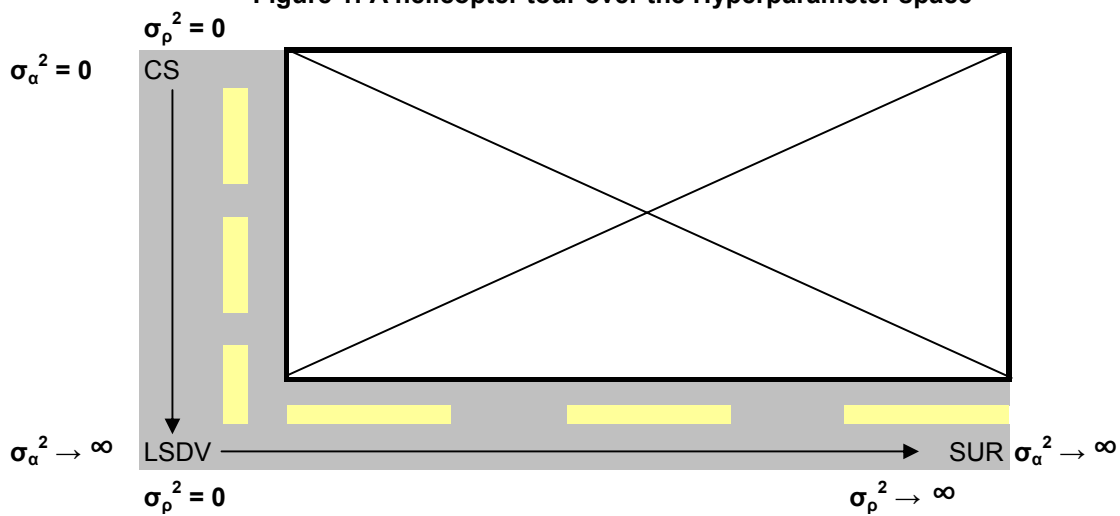


Figure 2: σ -convergence.

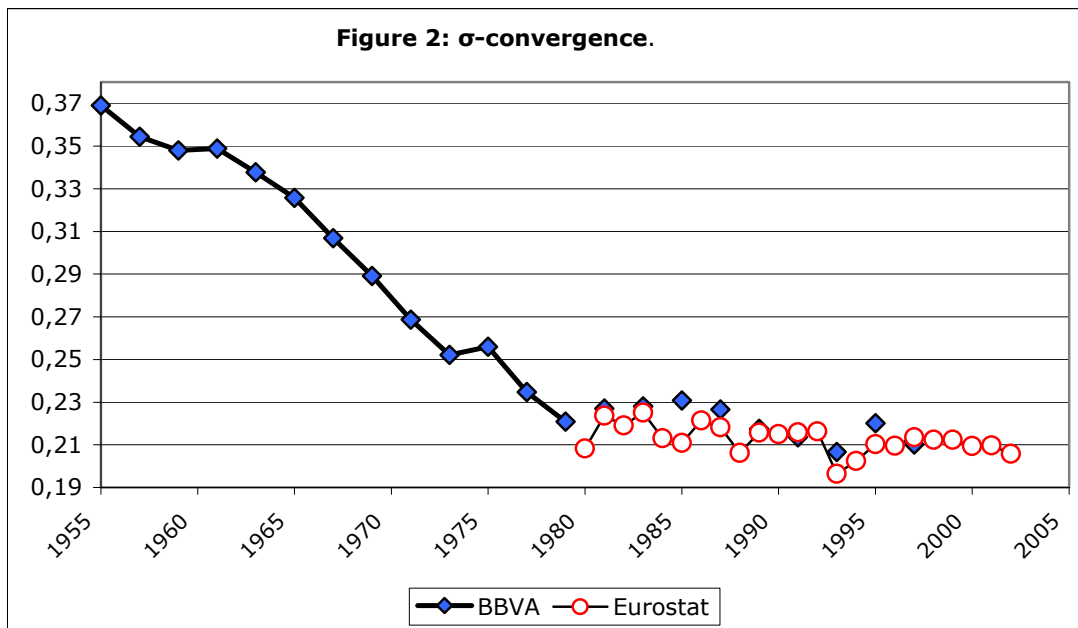


Table 1: Corner cases

| | CS ($\sigma_a^2 = 10^{-6}$, $\sigma_p^2 = 10^{-6}$) | | | | LSDV ($\sigma_a^2 = 10^6$, $\sigma_p^2 = 10^{-6}$) | | | | SUR ($\sigma_a^2 = 10^6$, $\sigma_p^2 = 10^6$) | | | |
|--------------------|--|--------|-------------------|----------|---|--------|-------------------|----------|---|--------|-------------------|----------|
| | α | ρ | $\alpha/(1-\rho)$ | $1-\rho$ | α | ρ | $\alpha/(1-\rho)$ | $1-\rho$ | α | ρ | $\alpha/(1-\rho)$ | $1-\rho$ |
| Galicia | -0,0005 | 0,9979 | -0,2597 | 0,21% | -0,0844 | 0,5970 | -0,2095 | 40,30% | -0,0976 | 0,5324 | -0,2087 | 46,76% |
| Asturias | -0,0007 | 0,9978 | -0,3312 | 0,22% | -0,0451 | 0,5970 | -0,1120 | 40,30% | -0,0318 | 0,7397 | -0,1222 | 26,03% |
| Cantabria | 0,0004 | 0,9976 | 0,1599 | 0,24% | -0,0199 | 0,5968 | -0,0492 | 40,32% | -0,0132 | 0,7532 | -0,0537 | 24,68% |
| País Vasco | 0,0005 | 0,9979 | 0,2139 | 0,21% | 0,0834 | 0,5971 | 0,2071 | 40,29% | 0,1120 | 0,4591 | 0,2071 | 54,09% |
| Navarra | -0,0003 | 0,9978 | -0,1581 | 0,22% | 0,0898 | 0,5971 | 0,2228 | 40,29% | 0,1438 | 0,3564 | 0,2234 | 64,36% |
| Rioja | -0,0002 | 0,9978 | -0,0965 | 0,22% | 0,0597 | 0,5970 | 0,1481 | 40,30% | 0,0540 | 0,6323 | 0,1470 | 36,77% |
| Aragón | 0,0007 | 0,9980 | 0,3533 | 0,20% | 0,0215 | 0,5970 | 0,0534 | 40,30% | 0,0300 | 0,4197 | 0,0518 | 58,03% |
| Madrid | 0,0016 | 0,9983 | 0,9552 | 0,17% | 0,1064 | 0,5972 | 0,2642 | 40,28% | 0,0367 | 0,8793 | 0,3041 | 12,07% |
| Castilla-León | 0,0002 | 0,9979 | 0,0799 | 0,21% | -0,0294 | 0,5971 | -0,0729 | 40,29% | -0,0124 | 0,8411 | -0,0780 | 15,89% |
| Castilla-La Mancha | 0,0000 | 0,9979 | -0,0134 | 0,21% | -0,0877 | 0,5970 | -0,2175 | 40,30% | -0,0264 | 0,8838 | -0,2274 | 11,62% |
| Extremadura | 0,0001 | 0,9978 | 0,0594 | 0,22% | -0,1919 | 0,5970 | -0,4763 | 40,30% | -0,1013 | 0,7815 | -0,4634 | 21,85% |
| Cataluña | -0,0005 | 0,9979 | -0,2386 | 0,21% | 0,0696 | 0,5971 | 0,1726 | 40,29% | 0,0650 | 0,6248 | 0,1734 | 37,52% |
| Valencia | -0,0007 | 0,9978 | -0,3027 | 0,22% | -0,0062 | 0,5971 | -0,0155 | 40,29% | -0,0055 | 0,6715 | -0,0166 | 32,85% |
| Baleares | 0,0002 | 0,9980 | 0,0954 | 0,20% | 0,0882 | 0,5970 | 0,2189 | 40,30% | 0,0770 | 0,6481 | 0,2188 | 35,19% |
| Andalucía | -0,0006 | 0,9979 | -0,2743 | 0,21% | -0,1143 | 0,5970 | -0,2837 | 40,30% | -0,2471 | 0,1207 | -0,2810 | 87,93% |
| Murcia | -0,0002 | 0,9979 | -0,0921 | 0,21% | -0,0671 | 0,5971 | -0,1667 | 40,29% | -0,0323 | 0,8089 | -0,1692 | 19,11% |
| Canarias | -0,0004 | 0,9980 | -0,1944 | 0,20% | -0,0145 | 0,5973 | -0,0360 | 40,27% | -0,0039 | 0,7999 | -0,0195 | 20,01% |

Table 2: Intermediate cases (between CS and LSDV)

| PRIOR | σ_a^2 | | σ_p^2 | | σ_a^2 | | σ_p^2 | | σ_a^2 | | σ_p^2 | | σ_a^2 | | σ_p^2 | |
|--------------------|--------------|--------|--------------|--------|--------------|--------|--------------|--------|--------------|--------|--------------|--------|--------------|--------|--------------|--------|
| | 10^{-5} | | 10^{-6} | | 10^{-4} | | 10^{-6} | | 10^{-3} | | 10^{-6} | | 10^{-2} | | 10^{-6} | |
| | α | ρ | α | ρ | α | ρ | α | ρ | α | ρ | α | ρ | α | ρ | α | ρ |
| Galicia | -0,0020 | 0,9949 | -0,0083 | 0,9613 | -0,0226 | 0,8960 | -0,0431 | 0,7990 | -0,0754 | 0,6414 | -0,0844 | 0,5979 | | | | |
| Asturias | -0,0034 | 0,9948 | -0,0079 | 0,9613 | -0,0158 | 0,8960 | -0,0260 | 0,7991 | -0,0409 | 0,6414 | -0,0451 | 0,5979 | | | | |
| Cantabria | 0,0010 | 0,9946 | -0,0027 | 0,9611 | -0,0068 | 0,8958 | -0,0113 | 0,7989 | -0,0180 | 0,6412 | -0,0198 | 0,5978 | | | | |
| País Vasco | 0,0017 | 0,9949 | 0,0063 | 0,9613 | 0,0203 | 0,8961 | 0,0414 | 0,7991 | 0,0743 | 0,6415 | 0,0833 | 0,5981 | | | | |
| Navarra | -0,0012 | 0,9949 | 0,0034 | 0,9614 | 0,0207 | 0,8961 | 0,0439 | 0,7991 | 0,0797 | 0,6415 | 0,0896 | 0,5981 | | | | |
| Rioja | -0,0011 | 0,9949 | 0,0001 | 0,9614 | 0,0105 | 0,8961 | 0,0270 | 0,7991 | 0,0524 | 0,6414 | 0,0595 | 0,5979 | | | | |
| Aragón | 0,0026 | 0,9950 | 0,0066 | 0,9615 | 0,0087 | 0,8961 | 0,0122 | 0,7991 | 0,0195 | 0,6414 | 0,0215 | 0,5980 | | | | |
| Madrid | 0,0056 | 0,9951 | 0,0138 | 0,9615 | 0,0312 | 0,8962 | 0,0563 | 0,7992 | 0,0955 | 0,6416 | 0,1062 | 0,5981 | | | | |
| Castilla-León | 0,0005 | 0,9949 | 0,0009 | 0,9614 | -0,0057 | 0,8961 | -0,0147 | 0,7992 | -0,0262 | 0,6415 | -0,0293 | 0,5980 | | | | |
| Castilla-La Mancha | -0,0011 | 0,9950 | -0,0055 | 0,9614 | -0,0216 | 0,8961 | -0,0441 | 0,7991 | -0,0780 | 0,6414 | -0,0873 | 0,5980 | | | | |
| Extremadura | 0,0009 | 0,9949 | -0,0046 | 0,9615 | -0,0387 | 0,8961 | -0,0913 | 0,7991 | -0,1699 | 0,6415 | -0,1913 | 0,5980 | | | | |
| Cataluña | 0,0009 | 0,9951 | 0,0079 | 0,9616 | 0,0197 | 0,8962 | 0,0363 | 0,7991 | 0,0623 | 0,6415 | 0,0695 | 0,5980 | | | | |
| Valencia | -0,0022 | 0,9949 | -0,0041 | 0,9614 | -0,0041 | 0,8961 | -0,0043 | 0,7991 | -0,0058 | 0,6415 | -0,0062 | 0,5980 | | | | |
| Baleares | 0,0006 | 0,9950 | 0,0064 | 0,9615 | 0,0221 | 0,8962 | 0,0440 | 0,7992 | 0,0783 | 0,6415 | 0,0878 | 0,5980 | | | | |
| Andalucía | -0,0021 | 0,9949 | -0,0107 | 0,9614 | -0,0305 | 0,8960 | -0,0580 | 0,7990 | -0,1019 | 0,6414 | -0,1141 | 0,5979 | | | | |
| Murcia | -0,0015 | 0,9949 | -0,0092 | 0,9614 | -0,0205 | 0,8961 | -0,0345 | 0,7991 | -0,0599 | 0,6415 | -0,0671 | 0,5980 | | | | |
| Canarias | -0,0002 | 0,9951 | 0,0017 | 0,9615 | 0,0008 | 0,8962 | -0,0039 | 0,7993 | -0,0121 | 0,6417 | -0,0143 | 0,5982 | | | | |

Table 3: Intermediate cases (between LSDV and SUR)

| PRIOR | σ_a^2 | | σ_p^2 | | σ_a^2 | | σ_p^2 | | σ_a^2 | | σ_p^2 | | σ_a^2 | | σ_p^2 | |
|--------------------|--------------|-----------|--------------|-----------|--------------|-----------|--------------|-----------|--------------|-----------|--------------|---------|--------------|--------|--------------|--------|
| | 10^6 | 10^{-5} | 10^6 | 10^{-4} | 10^6 | 10^{-3} | 10^6 | 10^{-2} | 10^6 | 10^{-1} | 10^6 | 1 | | | | |
| | α | ρ | α | ρ | α | ρ | α | ρ | α | ρ | α | ρ | α | ρ | α | ρ |
| Galicia | -0,0852 | 0,5934 | -0,0974 | 0,5336 | -0,0726 | 0,6554 | -0,0837 | 0,6007 | -0,0982 | 0,5296 | -0,1129 | 0,4578 | | | | |
| Asturias | -0,0454 | 0,5935 | -0,0530 | 0,5126 | -0,0384 | 0,6680 | -0,0398 | 0,6548 | -0,0306 | 0,7527 | -0,0295 | 0,7643 | | | | |
| Cantabria | -0,0201 | 0,5919 | -0,0229 | 0,5250 | -0,0165 | 0,6760 | -0,0158 | 0,6948 | -0,0142 | 0,7322 | -0,0167 | 0,6714 | | | | |
| País Vasco | 0,0840 | 0,5951 | 0,0950 | 0,5417 | 0,0585 | 0,7180 | 0,0850 | 0,5903 | 0,1019 | 0,5084 | 0,1186 | 0,4277 | | | | |
| Navarra | 0,0902 | 0,5951 | 0,0992 | 0,5548 | 0,0673 | 0,6974 | 0,1166 | 0,4776 | 0,1510 | 0,3244 | 0,1756 | 0,2149 | | | | |
| Rioja | 0,0602 | 0,5936 | 0,0678 | 0,5462 | 0,0455 | 0,6852 | 0,0525 | 0,6418 | 0,0679 | 0,5453 | 0,0600 | 0,5950 | | | | |
| Aragón | 0,0217 | 0,5938 | 0,0254 | 0,5162 | 0,0211 | 0,6053 | 0,0279 | 0,4634 | 0,0345 | 0,3264 | 0,0352 | 0,3117 | | | | |
| Madrid | 0,1069 | 0,5953 | 0,1215 | 0,5362 | 0,0890 | 0,6677 | 0,0765 | 0,7185 | 0,0586 | 0,7908 | 0,0636 | 0,7703 | | | | |
| Castilla-León | -0,0294 | 0,5948 | -0,0330 | 0,5448 | -0,0211 | 0,7165 | -0,0132 | 0,8292 | -0,0113 | 0,8578 | -0,0168 | 0,7788 | | | | |
| Castilla-La Mancha | -0,0883 | 0,5937 | -0,1024 | 0,5280 | -0,0545 | 0,7521 | -0,0385 | 0,8274 | -0,0225 | 0,9017 | -0,0268 | 0,8820 | | | | |
| Extremadura | -0,1935 | 0,5939 | -0,2080 | 0,5643 | -0,1198 | 0,7435 | -0,1093 | 0,7652 | -0,0660 | 0,8533 | -0,1006 | 0,7826 | | | | |
| Cataluña | 0,0699 | 0,5948 | 0,0751 | 0,5631 | 0,0488 | 0,7231 | 0,0516 | 0,7064 | 0,0523 | 0,7021 | 0,0503 | 0,7138 | | | | |
| Valencia | -0,0063 | 0,5944 | -0,0069 | 0,5380 | -0,0054 | 0,6691 | -0,0065 | 0,5766 | -0,0056 | 0,6602 | -0,0062 | 0,5957 | | | | |
| Baleares | 0,0887 | 0,5940 | 0,1037 | 0,5251 | 0,0662 | 0,6977 | 0,0689 | 0,6853 | 0,0697 | 0,6814 | 0,0968 | 0,5570 | | | | |
| Andalucía | -0,1153 | 0,5935 | -0,1338 | 0,5273 | -0,0960 | 0,6627 | -0,0913 | 0,6794 | -0,1776 | 0,3699 | -0,2826 | -0,0069 | | | | |
| Murcia | -0,0676 | 0,5947 | -0,0767 | 0,5393 | -0,0535 | 0,6807 | -0,0567 | 0,6604 | -0,0458 | 0,7271 | -0,0447 | 0,7342 | | | | |
| Canarias | -0,0145 | 0,5965 | -0,0157 | 0,5728 | -0,0072 | 0,7355 | -0,0021 | 0,8326 | -0,0019 | 0,8370 | -0,0031 | 0,8146 | | | | |

Table 4: A comparison with Canova-Marcet's approach

| Prior | | Canova-Marcet | | | This paper | |
|--------------|--------------|-----------------|----------------|-------------------|----------------|-------------------|
| σ_a^2 | σ_p^2 | σ_{ML}^2 | log-likelihood | mean(1 - ρ) | log-likelihood | mean(1 - ρ) |
| 10^{-6} | 10^{-6} | 4,87E-04 | 892,5 | 0,65% | 1155,4 | 0,21% |
| 10^{-5} | 10^{-6} | 4,92E-04 | 894,4 | 0,79% | 1169,7 | 0,51% |
| 10^{-4} | 10^{-6} | 4,83E-04 | 900,7 | 2,10% | 1179,0 | 3,86% |
| 10^{-3} | 10^{-6} | 4,09E-04 | 915,9 | 10,28% | 1190,1 | 10,39% |
| 10^{-2} | 10^{-6} | 4,05E-04 | 923,0 | 18,69% | 1191,9 | 20,09% |
| 10^{-1} | 10^{-6} | 4,06E-04 | 923,3 | 20,39% | 1193,0 | 35,85% |
| 1 | 10^{-6} | 4,06E-04 | 923,3 | 20,57% | 1193,3 | 40,20% |
| 10^{+6} | 10^{-6} | 4,06E-04 | 923,3 | 20,60% | 1193,3 | 40,29% |
| 10^{+6} | 10^{-5} | 4,06E-04 | 923,3 | 20,60% | 1194,0 | 40,58% |
| 10^{+6} | 10^{-4} | 4,05E-04 | 923,4 | 20,62% | 1221,6 | 46,06% |
| 10^{+6} | 10^{-3} | 4,34E-04 | 923,9 | 20,78% | 1219,6 | 30,86% |
| 10^{+6} | 10^{-2} | 4,23E-04 | 927,4 | 21,93% | 1238,4 | 32,91% |
| 10^{+6} | 10^{-1} | 3,90E-04 | 932,4 | 25,03% | 1248,4 | 34,70% |
| 10^{+6} | 1 | 3,90E-04 | 933,5 | 26,82% | 1241,5 | 40,79% |
| 10^{+6} | 10^{+6} | 3,90E-04 | 933,5 | 27,16% | 1247,5 | 35,57% |

Table 5: Relative income per capita

| | BBVA | | Eurostat | |
|--------------------|---------|---------|----------|---------|
| | 1955 | 1979 | 1980 | 2002 |
| Galicia | -0,3945 | -0,2192 | -0,1467 | -0,2000 |
| Asturias | 0,0319 | 0,0124 | 0,0061 | -0,1579 |
| Cantabria | 0,0549 | 0,0416 | 0,0379 | -0,0248 |
| País Vasco | 0,4633 | 0,1507 | 0,2272 | 0,2305 |
| Navarra | 0,0522 | 0,0964 | 0,2386 | 0,2247 |
| Rioja | -0,0151 | 0,0712 | 0,2115 | 0,1026 |
| Aragón | -0,0582 | 0,0454 | 0,0076 | 0,0565 |
| Madrid | 0,6388 | 0,2640 | 0,1640 | 0,3158 |
| Castilla-León | -0,3381 | -0,1533 | -0,0234 | -0,0531 |
| Castilla-La Mancha | -0,6025 | -0,2656 | -0,1838 | -0,2187 |
| Extremadura | -0,6681 | -0,4999 | -0,5552 | -0,4189 |
| Cataluña | 0,3802 | 0,2198 | 0,1187 | 0,1922 |
| Valencia | 0,0603 | 0,0275 | 0,0002 | -0,0416 |
| Baleares | 0,2592 | 0,3473 | 0,1544 | 0,1616 |
| Andalucía | -0,3619 | -0,2968 | -0,2328 | -0,2770 |
| Murcia | -0,3677 | -0,1559 | -0,1587 | -0,1790 |
| Canarias | -0,2369 | -0,0651 | -0,1933 | -0,0481 |
| Standard Deviation | 0,3690 | 0,2209 | 0,2083 | 0,2059 |

Table 6: Persistence in inequalities

| Prior | | $SS_n = a + b \cdot y_{80,n}$ | | | | | |
|--------------|--------------|-------------------------------|-------|-----------------------|-------|-------|----------------|
| σ_a^2 | σ_p^2 | a_{OLS} t-statistic | | b_{OLS} t-statistic | | R^2 | mean(ρ) |
| 10^{-6} | 10^{-6} | 0,0047 | 0,06 | 0,3762 | 0,99 | 6,1% | 0,9979 |
| 10^{-5} | 10^{-6} | 0,0011 | 0,01 | 0,5041 | 0,97 | 5,9% | 0,9949 |
| 10^{-4} | 10^{-6} | 0,0021 | 0,06 | 0,5468 | 3,07 | 38,6% | 0,9614 |
| 10^{-3} | 10^{-6} | -0,0019 | -0,08 | 0,8433 | 6,95 | 76,3% | 0,8961 |
| 10^{-2} | 10^{-6} | -0,0026 | -0,13 | 0,9269 | 9,15 | 84,8% | 0,7991 |
| 10^{-1} | 10^{-6} | -0,0025 | -0,13 | 0,9437 | 10,30 | 87,6% | 0,6415 |
| 1 | 10^{-6} | -0,0025 | -0,13 | 0,9454 | 10,47 | 88,0% | 0,5980 |
| 10^{+6} | 10^{-6} | -0,0025 | -0,14 | 0,9459 | 10,48 | 88,0% | 0,5971 |
| 10^{+6} | 10^{-5} | -0,0025 | -0,13 | 0,9458 | 10,49 | 88,0% | 0,5942 |
| 10^{+6} | 10^{-4} | -0,0023 | -0,13 | 0,9461 | 10,64 | 88,3% | 0,5394 |
| 10^{+6} | 10^{-3} | -0,0021 | -0,11 | 0,9380 | 9,98 | 86,9% | 0,6914 |
| 10^{+6} | 10^{-2} | -0,0012 | -0,06 | 0,9355 | 9,65 | 86,1% | 0,6709 |
| 10^{+6} | 10^{-1} | -0,0007 | -0,03 | 0,9262 | 9,25 | 85,1% | 0,6530 |
| 10^{+6} | 1 | -0,0013 | -0,07 | 0,9356 | 9,57 | 85,9% | 0,5921 |
| 10^{+6} | 10^{+6} | -0,0003 | -0,01 | 0,9433 | 9,34 | 85,3% | 0,6443 |

Table 7: Too many priors?

| j | Prior | | $d(j, y_{80})$ $d(j, SS)$ | | mean(ρ) |
|----|--------------|--------------|---------------------------|--------|----------------|
| | σ_a^2 | σ_p^2 | | | |
| 1 | 10^{-6} | 10^{-6} | 0,2413 | 0,9864 | 0,9979 |
| 2 | 10^{-5} | 10^{-6} | 0,2472 | 0,7918 | 0,9949 |
| 3 | 10^{-4} | 10^{-6} | 0,1745 | 0,1312 | 0,9614 |
| 4 | 10^{-3} | 10^{-6} | 0,1186 | 0,0516 | 0,8961 |
| 5 | 10^{-2} | 10^{-6} | 0,0934 | 0,0369 | 0,7991 |
| 6 | 10^{-1} | 10^{-6} | 0,0799 | 0,0296 | 0,6415 |
| 7 | 1 | 10^{-6} | 0,0781 | 0,0288 | 0,5980 |
| 8 | 10^{+6} | 10^{-6} | 0,0781 | 0,0289 | 0,5971 |
| 9 | 10^{+6} | 10^{-5} | 0,0781 | 0,0290 | 0,5942 |
| 10 | 10^{+6} | 10^{-4} | 0,0760 | 0,0278 | 0,5394 |
| 11 | 10^{+6} | 10^{-3} | 0,0830 | 0,0314 | 0,6914 |
| 12 | 10^{+6} | 10^{-2} | 0,0854 | 0,0320 | 0,6709 |
| 13 | 10^{+6} | 10^{-1} | 0,0925 | 0,0390 | 0,6530 |
| 14 | 10^{+6} | 1 | 0,0864 | 0,0322 | 0,5921 |
| 15 | 10^{+6} | 10^{+6} | 0,0915 | 0,0341 | 0,6443 |